

- (1) Compute the homology groups of the torus $S^1 \times S^1$.
- (2) The **suspension** of a space X , denoted SX , is $X \times I / \sim$ where $(x, 1) \sim (x', 1)$ and $(x, 0) \sim (x', 0)$ for all $x, x' \in X$.
Prove that $\tilde{H}_{n+1}(SX) \cong \tilde{H}_n(X)$.
- (3) Compute the homology groups $H_n(X, A)$ when X is S^2 or $S^1 \times S^1$ and A is a finite set of points.
- (4) (a) Show that the quotient map $S^1 \times S^1 \rightarrow S^2$ collapsing the subspace $S^1 \vee S^1$ to a point is not nullhomotopic by showing that it induces an isomorphism on H_2 .
(b) Show via covering spaces that any map $S^2 \rightarrow S^1 \times S^1$ is nullhomotopic.