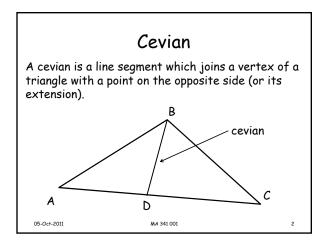
Cevians, Symmedians, and Excircles

MA 341 - Topics in Geometry Lecture 16

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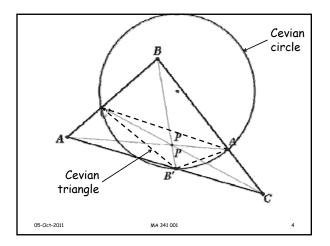
Cevian Triangle & Circle

- Pick P in the interior of $\triangle ABC$
- Draw cevians from each vertex through P to the opposite side
- Gives set of three intersecting cevians AA', BB', and CC' with respect to that point.
- The triangle $\Delta A'B'C'$ is known as the cevian triangle of ΔABC with respect to P
- Circumcircle of $\Delta A'B'C'$ is known as the evian circle with respect to P.

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Cevians In $\triangle ABC$ examples of cevians are: medians - cevian point = Gperpendicular bisectors - cevian point = O angle bisectors - cevian point = I (incenter) altitudes - cevian point = H Ceva's Theorem deals with concurrence of any set of cevians.

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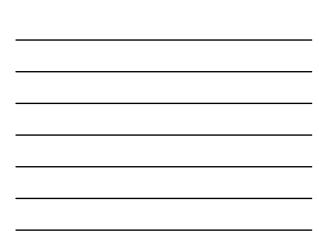
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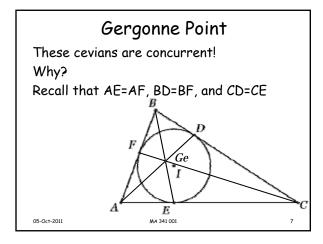
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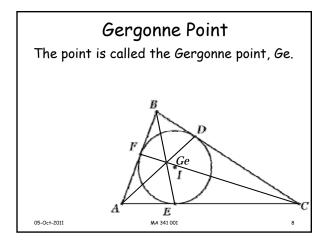
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Gergonne Point In ΔABC find the incircle and points of tangency of incircle with sides of $\triangle ABC$. Known as contact triangle F **E** MA 341 001 A

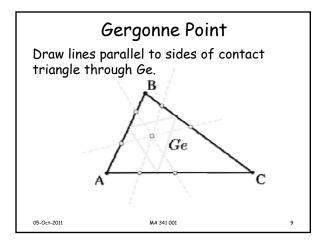




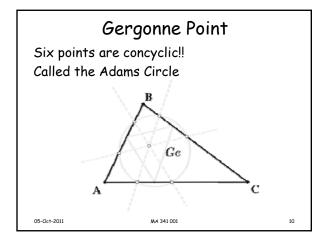




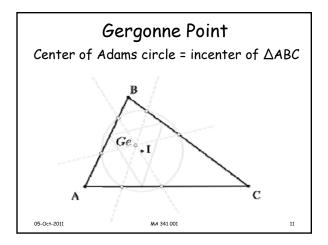




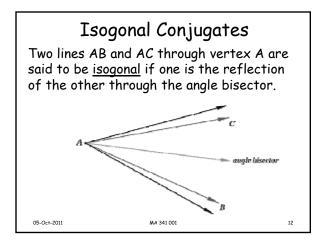














Isogonal Conjugates

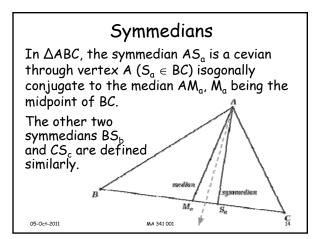
If lines through A, B, and C are concurrent at P, then the isogonal lines are concurrent at Q.

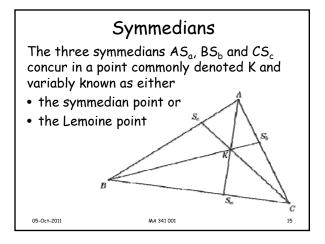
Points P and Q are <u>isogonal conjugates</u>.

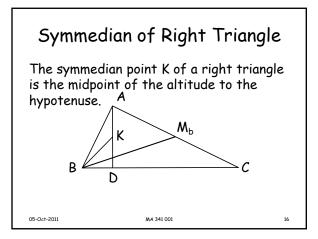
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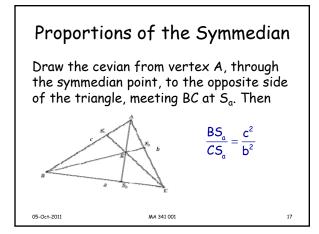
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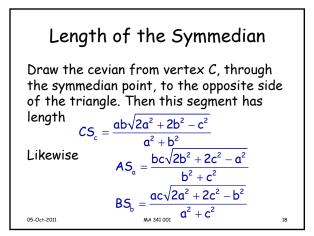


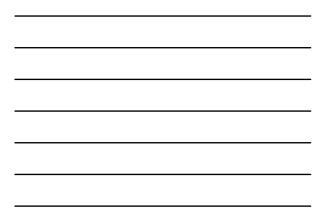


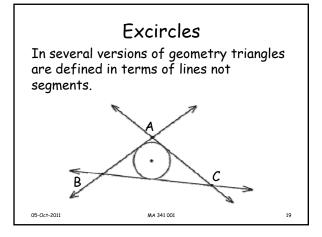




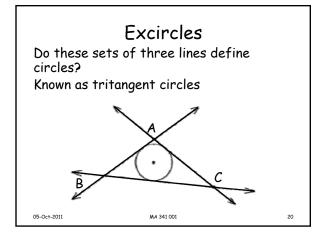




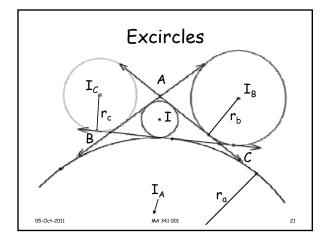




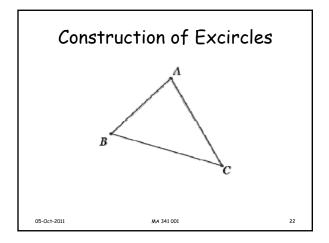




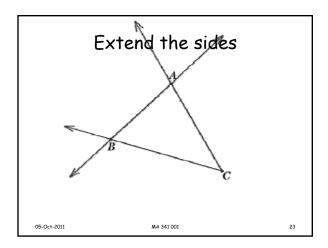




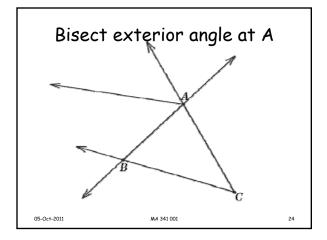




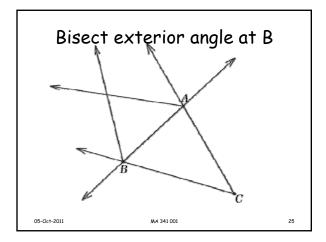




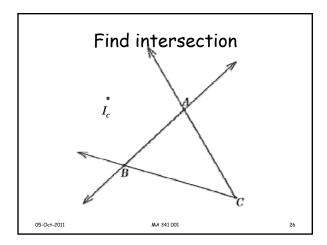




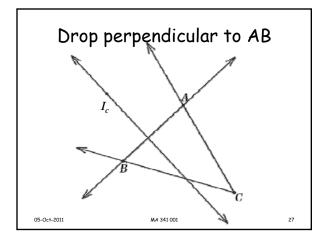




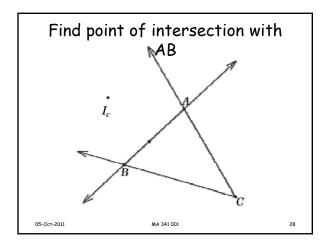




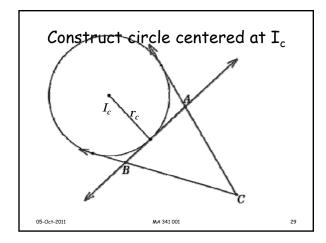




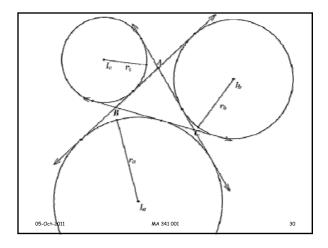




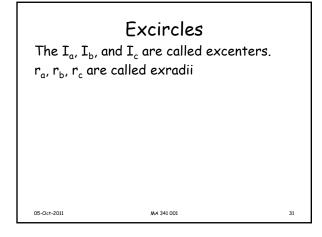












Excircles

Theorem: The length of the tangent from a vertex to the opposite exscribed circle

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equals the semiperimeter, s.

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