MA 114 Worksheet #23: Polar coordinates

- 1. Convert from rectangular to polar coordinates:
 - (a) $(1,\sqrt{3})$
 - (b) (-1, 0)
 - (c) (2, -2)
- 2. Convert from polar to rectangular coordinates:

(a)
$$\left(2, \frac{\pi}{6}\right)$$

(b) $\left(-1, \frac{\pi}{2}\right)$
(c) $\left(1, -\frac{\pi}{4}\right)$

- 3. List all the possible polar coordinates for the point whose polar coordinates are $(-2, \pi/2)$.
- 4. Sketch the graph of the polar curves:
 - (a) $\theta = \frac{3\pi}{4}$ (b) $r = \pi$ (c) $r = \cos \theta$ (d) $r = \cos(2\theta)$ (e) $r = 1 + \cos \theta$ (f) $r = 2 - 5 \sin \theta$

5. Find the equation in polar coordinates of the line through the origin with slope $\frac{1}{3}$.

- 6. Find the polar equation for:
 - (a) $x^{2} + y^{2} = 9$ (b) x = 4(c) y = 4(d) xy = 4
- 7. Convert the equation of the circle $r = 2\sin\theta$ to rectangular coordinates and find the center and radius of the circle.
- 8. Find the distance between the polar points $(3, \pi/3)$ and $(6, 7\pi/6)$.