## Chapter 2: Practice/review problems

The collection of problems listed below contains questions taken from previous MA123 exams.

## Average rates of change (Word Problems)

[1].	A train travels from $A$ to $B$ to $C$ . The distance from $A$ to $B$ is 10 miles and the distance from $B$ to	C is
	40 miles. The average velocity from $A$ to $B$ was 20 miles per hour and the average velocity from $B$	to $C$
	was 40 miles per hour. What was the average velocity from $A$ to $C$ in miles per hour?	

(a) 180/5

**(b)** 90/3

(c) 100/3

(d) 180/3

(e) 100/5

[2]. A train travels from city A to city B. It leaves city A at 10:30 am and arrives at city B at 1:30 pm. The distance between the cities is 150 miles. What was the average velocity of the train in miles per hour?

(a) 60

**(b)** 150

50

(d) 75

**(e)** 130

[3]. A train travels from city A to city B to city C. The distance from A to B is 20 miles. The distance from B to C is 45 miles. The train took 1 hour for the trip from A to B, stopped at city B for 30 minutes, and then went from B to C at an average velocity of 30 miles per hour. What was the average velocity of the train for the entire trip (in miles per hour)?

(a) 65

**(b)** 25

(c)  $\frac{65}{2}$  (d) 50

[4]. A train travels from A to B to C. The distance from A to B is 30 miles and the distance from B to C is 80 miles. The train leaves A at 10:00 AM and arrives at C at 3:00 PM. The average speed from A to B was 30 miles per hour. What was the average speed from B to C in miles per hour?

20 (a)

**(b)** 25

**(c)** 30

(d) 35

**(e)** 40

[5]. A train travels from city A to city B. The cities are 600 miles apart. The distance from city A at t hours after the train leaves A is given by  $d(t) = 50t + t^2$ .

What is the average velocity of the train in miles per hour during the trip from A to B?

(**Hint:** First find how long it takes for the train to get from A to B.)

(a) 50

**(b)** 55

60

(d) 65

**(e)** 70

[6]. John leaves at 9:00 am and drives from Lexington to Ashland arriving at 11:00 am. He stops for two hours since his girlfriend Mary is not yet ready. Then they drive together from Ashland to Columbus arriving at Columbus after a three-hour drive. The distance from Lexington to Ashland is 110 miles and the distance from Ashland to Columbus is 130 miles. Find the average velocity of John's car in miles per hour for the entire trip (including the two hour stop) correct to two decimal places.

(a) 33.81

**(b)** 33.42

(c) 35.00

34.29

(e) 34.47

## Average rates of change

[7].	If $g(x)$	$(x) = (x-1)^2$	what is the average	e rate	of change of	g(x) v	with respect to	o x as	x changes from $-3$ to $3$ ?
	(a)	-4	(b) -2	(c)	0	(d)	2	(e)	4
[8].	Supp	ose that $h(t)$	$=\frac{2}{t}$ . Find the ave	erage	rate of change	e of $h$	(t) from t = 5	o to t	= 10.
	(a)	05	(b)04	(c)	.05	(d)	.04	(e)	.02
[9].	Find	the average	rate of change of the	ne fun	action $R(t) =$	$\sqrt{2t}$	+7 as $t$ chang	es fro	om 1 to 9.
	(a)	$\frac{1}{3}$	(b) $\frac{1}{2}$	(c)	$\frac{1}{4}$	(d)	4	(e)	2
[10].	If $g(x)$	$x) =  x - 7  \le$	that is the average	rate	of change of $g$	y(x) w	rith respect to	x as	x changes from $-3$ to $3$ ?
	(a)	-2	<b>(b)</b> -1	(c)	0	(d)	1	(e)	2
[11].	Find	the average	rate of change of the	ne fun	action $G(t) =$	$ t^2 -$	1 as $t$ change	es fro	m-1 to 2.
	(a)	0	<b>(b)</b> 1	(c)	2	(d)	3	(e)	4
[12].	Let <i>g</i> 8.	$y(s) = s^2 - 3s$	+1. Find a value	$A \ge 0$	such that the	e avera	age rate of ch	ange	of $g(s)$ from 0 to $A$ equals
	(a)	0	<b>(b)</b> 8	(c)	11	(d)	15	(e)	22
[13].		$ext{pose } f(t) = t^3$ equals 2.	+ 1. Find a value	A  gre	ater than 0 su	ich th	at the averag	ge rate	e of change of $f(t)$ from 0
	(a)	1	(b) $\sqrt{2}$	(c)	$\sqrt{3}$	(d)	2	(e)	$\sqrt{5}$
				Diff	ference quot	ients	3		
<b>[14].</b>	Com	pute $\frac{f(2+h)}{h}$	$\frac{1-f(2)}{h}$ where $f(x)$	(c) = 3	$x^2 + 1.$				
	(a)	12	<b>(b)</b> 12 + h	(c)	12 + 2h	(d)	12 + 3h	(e)	None of the above
[15].	Wha	t is the avera	ge rate of change of	of $g(s)$	$= s^2 - 4 \text{ as } .$	s char	nges from 1 to	o 1 +	h?

(a) 9-h (b) 9+h (c) 9 (d) 9-2h (e) 9+2h

[16]. Let  $f(x) = 2x^2 - 3x$ . Find the average rate of change of f(x) from x = 3 to x = 3 + h.

(c) 4 + 2h

(b)

(a) 6 + 3h

2 + h

**(d)** 2

**(e)** h

	(a)	$h^2 - 2h$	(b)	h+2	(c)	$h^2 + 2h$	(d)	h-2	(e)	1
[18].	If f(	$t) = 3t^2 + 4 t$	hen			$\frac{f(1+h)-j}{h}$	$\frac{f(1)}{f(1)} = \frac{f(1)}{f(1)}$			
	(a)	4+3h	(b)	3+4h	(c)	6+3h	(d)	8+3h	(e)	8+4h
[19].	If f(	t) = 1/t then				$\frac{f(t+h)-j}{h}$	$\frac{f(t)}{}=$			
	(a)	$1/(h^2)$	(d)	1/(t(t-h))		1/(t(t+h))		!		-1/(t(t+h))
				Inst	antai	neous rates	of cha	ange		
[20].		sider a triangl				t $2x$ . Find the	ne insta	antaneous ra	ate of	change of the area of the
	(a)	1	(b)	2	(c)	5	(d)	10	(e)	20
[21].	Find	the instantar	neous	rate of chang	e of t	he function $F$	H(t) =	$t^3$ at $t=2$ .		
	(a)	2	(b)	3	(c)	8	(d)	12	(e)	27

If 
$$p(x) = Ax^2 + Bx + C$$
, then  $p'(x) = 2Ax + B$ .

[22]. If  $g(s) = 3s^2 + s - 2$  what is the value of g(s) when the instantaneous rate of change of g(s) with respect to s equals 1?

(a) -2 (b) -1 (c) 0 (d) 1 (e) 2

[23]. If  $g(s) = 3s^2 + 2s - 2$  what is the value of s for which the instantaneous rate of change of g(s) with respect to s equals 8?

(a) -2 (b) -1 (c) 0 (d) 1 (e) 2

[94]	Sun	oose the	e price of a good is give	on by the guad	ratic function $P(t)$	- 2 58 ± 1.	4+ ⊥ 01+ <sup>2</sup>	What is the
[44]•	Supp	JOSE THE	e price of a good is given	en by the quadi	and function $I(t)$	- 2.50 T .1	±t + .01t .	What is the
	insta	antaneo	us rate of change in the	e price when $t =$	: 3?			
	(a)	.18	<b>(b)</b> .20	(c) .22	(d) .24	(e)	26	
	_		2			_		

- [25]. Let  $g(x) = x^2 + 4x + 5$ . Find a value of c between 1 and 10 such that the average rate of change of g(x) from x = 1 to x = 10 is equal to the instantaneous rate of g(x) at x = c.
  - (a) 4.75 (b) 5.0 (c) 5.25 (d) 5.5 (e) 5.75
- [26]. Find a nonnegative number A such that the average rate of change of  $F(t) = t^2 2t + 1$  from t = 1 to t = A equals the instantaneous rate of change of F(t) at t = 2.
  - (a) A = 0 (b) A = 2 (c) A = 3 (d) A = 4 (e) A = 5
- [27]. Suppose the cost C(q) (in dollars) of producing a quantity q of a product equals

$$C(q) = 500 + 2q + \frac{1}{5}q^2.$$

The marginal cost MC(q) equals the instantaneous rate of change of the total cost. Find the marginal cost when a quantity of 10 items are being produced.

## Tangent lines

- [28]. Find the slope of the tangent line to the graph of  $f(x) = 3x^2 7x + 4$  at x = 2.
  - (a) 5 (b) 6 (c) 7 (d) 8 (e) 9
- [29]. Find the equation of a line tangent to the curve  $y = 2x^2 + x + 1$  at x = 2.

(a) 
$$y = 9 + 11(x - 2)$$
 (b)  $y = 11 + 9(x - 2)$  (c)  $y = 22 + 13(x - 3)$  (d)  $y = 13 + 22(x - 3)$  (e)  $y = 7 + (4x + 1)$ 

- [30]. Suppose  $G(x) = x^2 + x 2$ . For what value of x is the tangent line to the graph of y = G(x) parallel to the x-axis?
  - (a) x = -1 (b) x = 0 (c) x = 2 (d) x = 1/2 (e) x = -1/2
- [31]. Suppose  $g(s) = s^2 + 4s + 1$ . Find a point of the graph of t = g(s) such that the tangent line to the graph is parallel to the s-axis.
  - (a) (2,9) (b) (-1,-2) (c) (-2,-3) (d) (-4,8) (e) (-4,1)

[32].	What is	the value	of $x$ s	such that the	slope	of the tange	nt lin	e to the grap	$h  ext{ of } f$	$f(x) = x^2 - 10x + 14$ is 6?	
	(a) 6		(b)	7	(c)	8	(d)	9	(e)	There is no such $x$	
[33].				Find a point equation $t =$		ne graph of $t$	=g(s)	s) such that t	the ta	ngent line to the graph is	
	(a) (0,	1)	(b)	(1/2, 5/4)	(c)	(1, 2)	(d)	(3/2, 13/4)	(e)	(2,5)	
						Velocity					
[34].	[34]. Suppose $h(t)$ represents the height of an object above the ground at time $t$ , where the height is measured in feet and the time $t$ is measured in seconds. If										
	$h(t) = -16t^2 + 48t + 144,$										
	what is the velocity of the object at time $t = 0$ ?										
	(a) 48 feet per second (b) 144 miles per hour (c) 32 furlongs per fortnight										
			(d)	64 feet per s	second	l	(e)	96 feet per s	second	l	
[35].	If $h(t)$ re	epresents	the he	ight of an ob	ject a	bove ground	level	at time $t$ and	h(t)	is given by	
					h	$(t) = -16t^2 +$	- 96t -	+ 1,			
	find the	height of	the ob	ject at the t	ime w	hen the velo	city is	zero.			
	(a) 144	4	(b)	145	(c)	148	(d)	150	(e)	160	
[36]. Suppose the position $P(t)$ of an object at time $t$ is given by $t^2 + 1$ . Find a value of $t$ at which instantaneous velocity of the object equals the average velocity on the interval $[0,1]$ .											
	(a) 1	/2	(b)	1	(c)	3/2	(d)	2	(e)	5/2	