

Supplement: Practice/review problems

The collection of problems listed below contains questions taken from previous MA123 exams.

[1]. Suppose that  $f(x) = \ln(g(x))$ . Assume that  $g(5) = 3$  and  $g'(5) = 4$ . Find  $f'(5)$ .

- (a)  $5/3$       (b)  $3/5$        (c)  $4/3$       (d)  $3/4$       (e) Does not exist

[2]. Suppose that  $f(x) = e^{g(x)}$ . Assume that  $g(5) = 3$  and  $g'(5) = 5$ . Find  $f'(5)$ .

- (a)  $5e^4$        (b)  $5e^3$       (c)  $3e^5$       (d)  $4e^3$       (e)  $3e^4$

[3]. Find  $f'(-1)$  where  $f(x) = \frac{x}{e^x}$ .

- (a)  $e^{-2}$       (b)  $-e^{-2}$        (c)  $2e$       (d)  $-2e$       (e)  $-e^{-1}$

[4]. Find the equation of the tangent line to the graph of  $f(x) = x^2e^x$  at  $x = 1$ .

- (a)  $y = 3ex + 2e$       (b)  $y = 2ex + 3e$        (c)  $y = 3ex - 2e$   
 (d)  $y = 2ex - 3e$       (e)  $y = 2ex - e$

[5]. Suppose that  $Q(t) = Q_0e^{rt}$ . Assume that  $(0, 5)$  lies on the graph of  $Q(t)$ . Assume also that the slope of the tangent line to the graph of  $Q(t)$  at  $t = 0$  is 10. Find  $r$ .

- (a) 1       (b) 2      (c)  $e$       (d) 5      (e) 10

[6]. The number of bacteria in a sample  $t$  hours from now is given by  $Q(t) = Q_0e^{kt}$ . If  $Q(0) = 10,000$  and  $Q'(0) = 20,000$ , how many bacteria are there in 4 hours?

- (a)  $10,000e^6$        (b)  $10,000e^8$       (c)  $10,000e^{10}$       (d)  $10,000e^{12}$       (e)  $10,000e^{16}$

[7]. How many years will it take an investment to triple in value if the interest rate is 4% compounded continuously?

- (a)  $\frac{\ln(3)}{.04}$       (b) 75      (c)  $\frac{\ln(.04)}{3}$       (d)  $\frac{3}{\ln(4)}$       (e)  $\frac{\ln(3)}{4}$