

## Homework 7, Sta 531 Fall 2008

Due 10/6

1. If  $X$  and  $Y$  are two independent r.v.s having  $\exp(\lambda_1)$  and  $\exp(\lambda_2)$  distributions, show that  $Z = \min(X, Y)$  is also an exponential r.v. Identify the parameter of  $Z$ .
2. Problem 4.47
3. Suppose the joint density function of  $(X, Y)$  is given as in Example 4.1.12 (page 146)  
Find the two marginal densities, and the two conditional densities.
4. In the context above, find  $E(X|Y)$  and verify  $E[E(X|Y)] = E(X)$ .
5. Let  $U = Y - X; V = X$ , where  $(X, Y)$  is given above, find the joint density of  $(U, V)$ .